## Mathematics homework \#1

Homework consists of 8 exercises. Exercises are numbered and title with their topics are marked near the number. Hints are provided to make solution process easier.

Exercise statements use parameters $a, b, c$, etc. to make tasks distinct for different students. List of parameter values is present in table 1 in appendix $A$.

Solutions should be handwritten with rather thorough explanations regarding notation introduced by the student (i.e. what are the events $A, B$ etc.) and chosen ways to solve the problems. Each solution should start with the exercise statement with the individual parameter values.

Solutions should be labeled with student name and the individual number (according to table 1 of the appendix A), group number and homework number.

The pictures of every solution should be taken and sent to lecturer's email Sergey.Garbar@novsu.ru, with subject including student's name with the individual number according to table 2 of the appendix A, group number and homework number.

Homework is recommended to be submitted before $20^{\text {th }}$ of December 2021.

## Exercise 1: Classical probability

A box contains marbles. There are $a$ red marbles, $b$ blue marbles, $c$ green marbles, $d$ yellow marbles and $e$ white marbles. What is the probability that the randomly chosen marble is $f$ ?

## Exercise 2: Complement of the event

A box contains marbles. There are $a$ red marbles, $b$ blue marbles, $c$ green marbles, $d$ yellow marbles and $e$ white marbles. What is the probability that the randomly chosen marble is not $g$ ?

Hint: how is this a complement event? What formula should be used here?

## Exercise 3: Compound events

A box contains marbles. There are $a$ red marbles, $b$ blue marbles, $c$ green marbles, $d$ yellow marbles and $e$ white marbles. Two marbles are consequently taken out of box at random. What is the probability that the first marble is $g$ and the second is $f$ ?

Hint: what kind of the compound event is considered here? What rule for finding the probability should be used?

## Exercise 4: Compound events

What is the probability that the card taken out of deck is $h$ or $i$ ?
Hint: what kind of the compound event is considered here? What rule for finding the probability should be used?

## Exercise 5: Counting rules

A person has $a$ scarfs, $b$ hats and $d$ jackets. How many ways to choose a scarf, a hat and a jacket does this person have?

## Exercise 6: Counting rules

A student has $c$ different notebooks and decided to give $a$ of them to a friend. How many ways does he have to give away these notebooks?

Hint: is that a permutation or a combination? Why?

## Exercise 7: Counting rules

A student has $d$ different notebooks and $a$ different subjects. How many ways does he have to assign a notebook to a subject?

Hint: is that a permutation or a combination? Why?

## Exercise 8: Total probability law

There were $b$ apples and $c$ oranges in the first basket. There are $d$ apples and $e$ oranges in the second basket. One basket is chosen. Probability to choose the first basket is $1 / a$. One fruit is taken out. What is the probability that this fruit is an apple?

Hint: what two steps can we split the experiment into? What are the probabilities of those steps?

## Appendix A: individual parameter values

Table 1 - Parameter values for exercises

| \# | Student name | $\boldsymbol{a}$ | b | c | d | $\boldsymbol{e}$ | $f$ | $g$ | $h$ | $i$ | $j$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Абуелмагд Халед Аттиа Вахба Гад | 2 | 5 | 13 | 10 | 12 | red | green | red | a number | lowercase |
| 2 | Али Мустафа Гамал Ахмед | 3 | 8 | 12 | 9 | 10 | green | blue | black | a face card | uppercase |
| 3 |  | 4 | 10 | 10 | 12 | 8 | blue | white | spades | an ace | lower and uppercase |
| 4 | Аль Бевани Мохаммед Акрам Кака Ахмед | 5 | 12 | 11 | 11 | 12 | white | yellow | clubs | an even number | lowercase |
| 5 | Мосса Мохамед Халафаллах Махвуз | 6 | 11 | 9 | 10 | 10 | yellow | red | hearts | a face card or 10 | uppercase |
| 6 | Мохамед Осама Сабер Хассан | 2 | 4 | 15 | 9 | 8 | red | green | diamonds | a number | lower and uppercase |
| 7 | Селим Мостафа Осман Ахмед | 3 | 5 | 14 | 12 | 12 | green | blue | red | a face card | lowercase |
| 8 | Мохамед Зияд Фагих Абделазиз | 4 | 8 | 13 | 11 | 10 | blue | white | black | an ace | uppercase |
| 9 | Саад Афаф Акмаль Морси | 5 | 10 | 12 | 10 | 8 | white | yellow | spades | an even number | lower and uppercase |
| 10 | Радниа Марьям Рамин | 6 | 12 | 10 | 9 | 12 | yellow | red | clubs | a face card or 10 | lowercase |
| 11 | Радния Амир Рамин | 2 | 11 | 11 | 12 | 10 | red | green | hearts | a number | uppercase |
| 12 | Шехата Мохамед Сами Заки | 3 | 4 | 9 | 11 | 8 | green | blue | diamonds | a face card | lower and uppercase |
| 13 | Шихата Ахмед Эльхилали Эльсаид Мохамед | 4 | 5 | 15 | 10 | 12 | blue | white | red | an ace | lowercase |
| 14 |  | 5 | 8 | 14 | 9 | 10 | white | yellow | black | an even number | uppercase |
| 15 |  | 6 | 10 | 13 | 12 | 8 | yellow | red | spades | a face card or 10 | lower and uppercase |
| 16 |  | 2 | 12 | 12 | 11 | 12 | red | green | clubs | a number | lowercase |


| $\#$ | Student name | $\boldsymbol{a}$ | $\boldsymbol{b}$ | $\boldsymbol{c}$ | $\boldsymbol{d}$ | $\boldsymbol{e}$ | $\boldsymbol{f}$ | $\boldsymbol{g}$ | $\boldsymbol{h}$ | $\boldsymbol{\boldsymbol { h }}$ | $\boldsymbol{j}$ |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 17 |  | 3 | 11 | 10 | 10 | 10 | green | blue | hearts | a face card | uppercase |
| 18 |  | 4 | 4 | 11 | 9 | 8 | blue | white | diamonds | an ace | lower and <br> uppercase |
| 19 |  | 5 | 5 | 9 | 12 | 12 | white | yellow | red | an even <br> number | lowercase |
| 20 |  | 6 | 8 | 15 | 11 | 10 | yellow | red | black | a face card <br> or 10 | uppercase |

